

Pulse shape optimization for electron-positron production

Florian Hebenstreit

Albert-Einstein-Center for Fundamental Physics, University of Bern



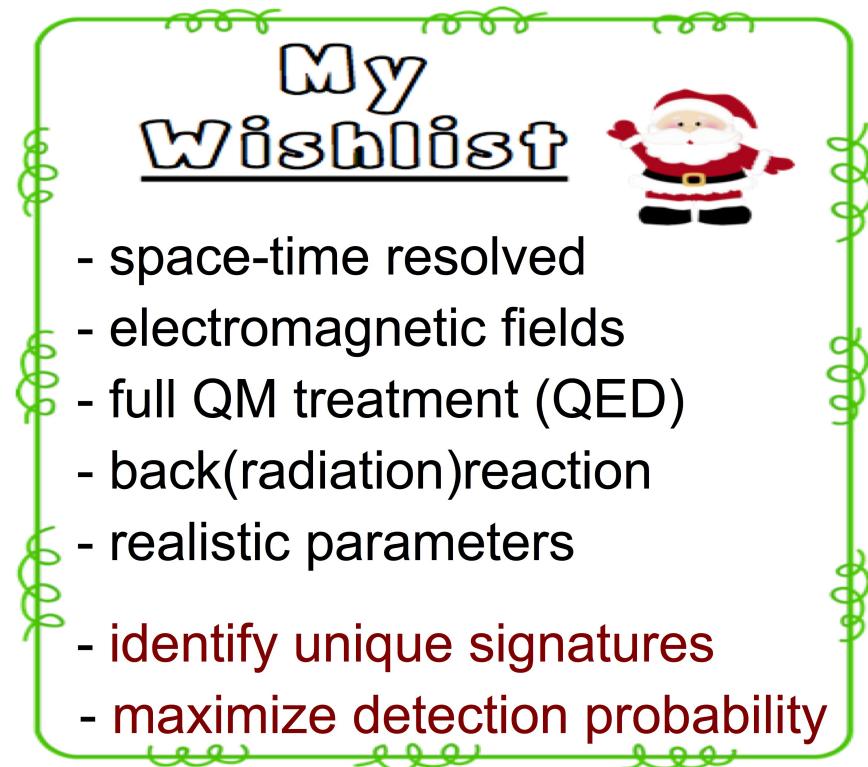
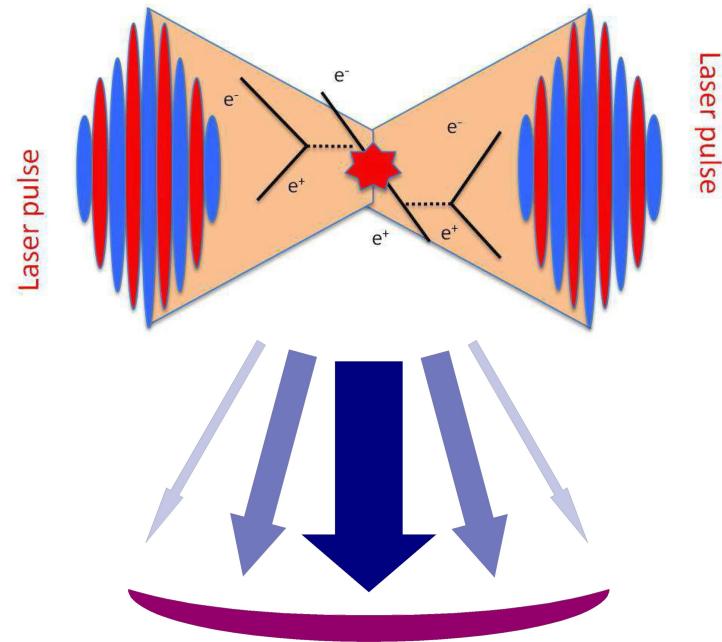
2nd Extremely High-Intensity Laser Physics Conference (ExHILP)
Lisbon, September 2017

- FH, *The inverse problem for Schwinger pair production*, **PLB 753** (2015)
- F. Fillion-Gourdeau, FH, D. Gagnon, and S. MacLean, *Pulse shape optimization for Schwinger pair production in rotating fields*, **PRD 96** (2017)

particle production & optimization strategies

electron-positron production

all-optical (colliding laser pulses)



You can't always get what you want

- spatial homogeneity
 - only electric fields
 - external-field approximation: classical field [800nm / 1J / $\sim 10^{20}$ photons]
 - no backreaction: low densities [no depletion or cascades]
- } focus of standing waves [matter of scales]

dynamical system (Vlasov) for given $E(t)$ determines $F(q,T)$

optimization strategies

- maximize a quantity that is determined by the distribution $F(q, T)$
[Kohlfürst, Mitter, von Winckel, FH and Alkofer, PRD 88 (2013)]

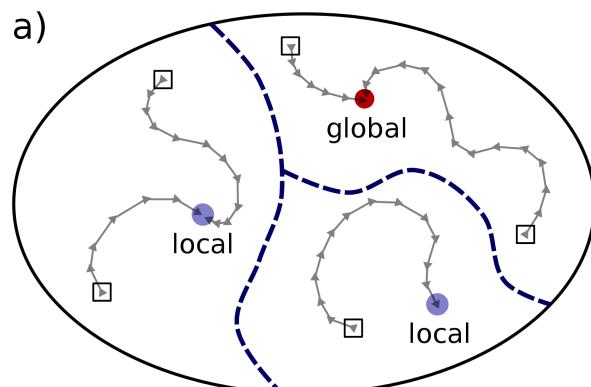
control function: $A(\{\phi_1, \dots, \phi_n\}; t)$ (vector potential \sim electric field)

cost functional: $J[F[A]; A]$ (e.g.: particle number) + constraints

global optimization problem:

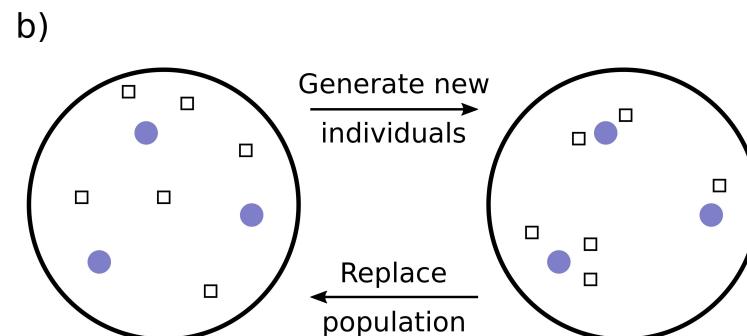
$$\tilde{J} = \max_{\{\phi_1, \dots, \phi_n\}} J[F[A]; A]$$

multistart + local search



ψ convex / few local extrema

population based metaheuristics



ψ global optimization strategy

the inverse problem

FH, *The inverse problem for Schwinger pair production*, **PLB 753 (2015)**

inverse problem for pair production

direct problem: given $E(t) \rightarrow$ solve for $F(q, T)$

inverse problems: which $E(t)$ results in a predetermined $F_0(q)$?

- why is this interesting/relevant?
 - theoretical: existence? # of necessary parameters? rate of convergence?
 - experimental: determine parameters to enhance detection probability
- inverse problems are typically ill-posed:
 - non-existence: solution does not exist
 - non-uniqueness: solution is not unique

} approximate solution is fine
} any 'good' configuration is fine

control function:

$$E(t) = \sum_{j=1}^n E_j \sin\left(\frac{\pi(t+T)j}{2T}\right)$$

harmonic superposition

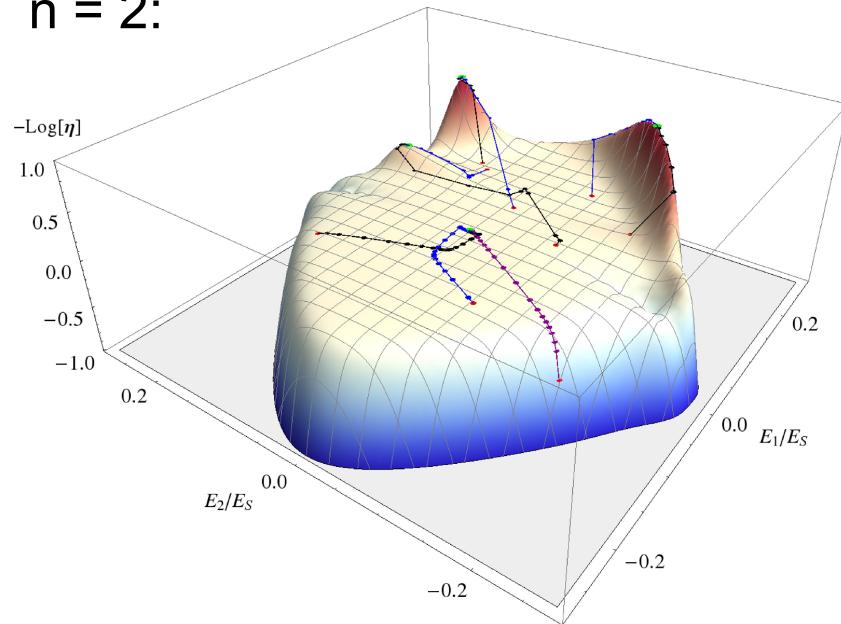
cost functional:

$$\eta_n = \frac{\int [dq] [F(q, T) - F_0(q)]^2}{\int [dq] F_0^2(q)}$$

least squares

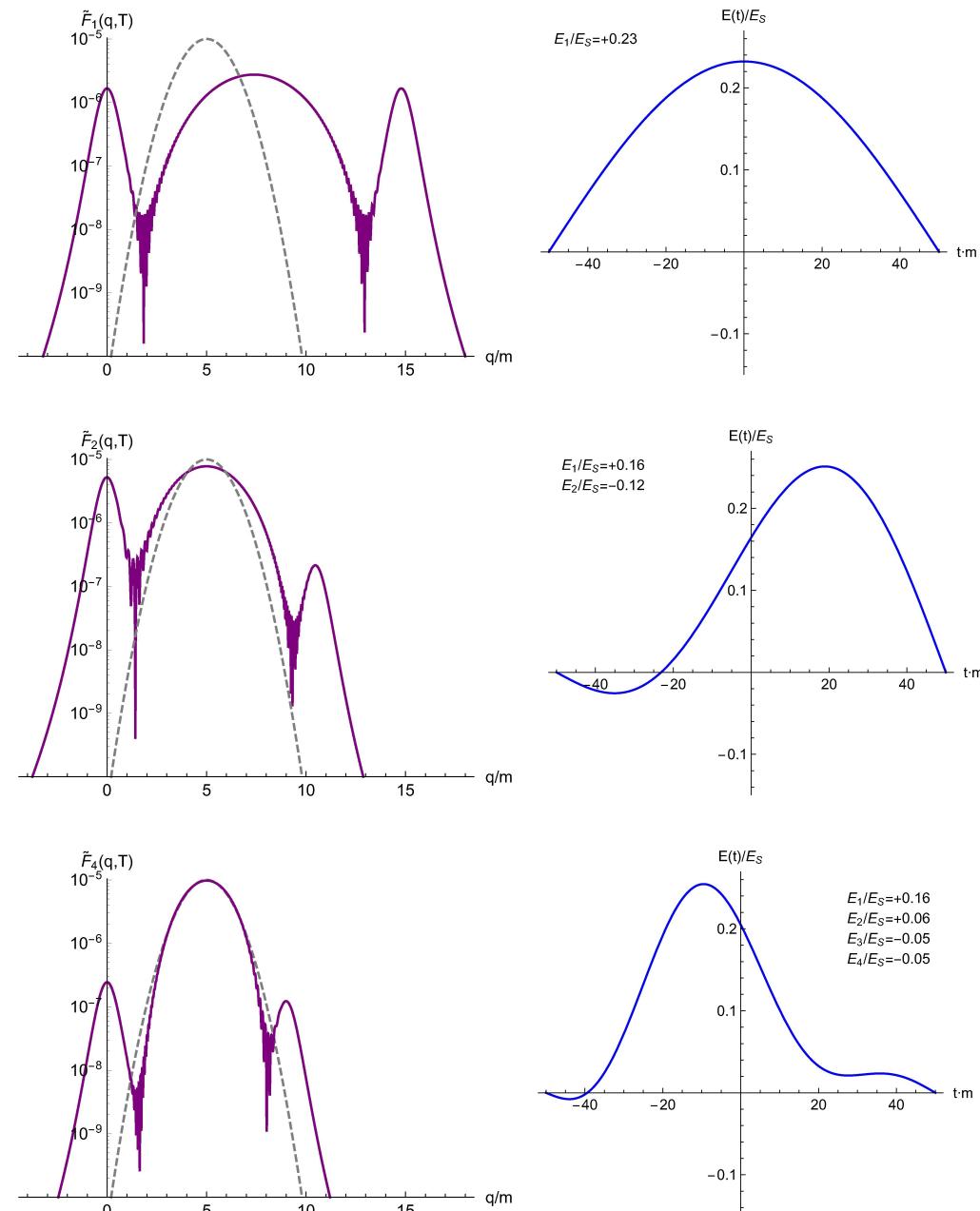
approximating spectral properties

$n = 2:$

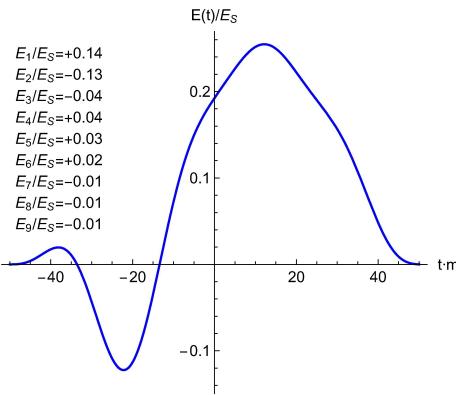
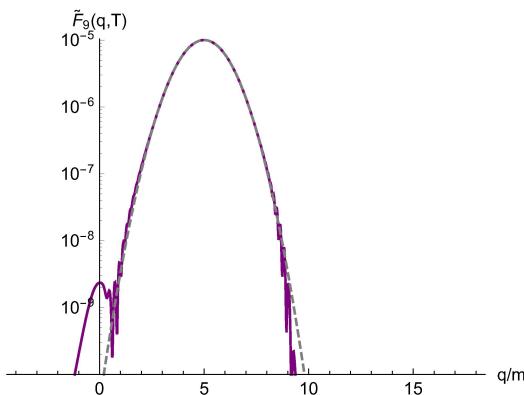
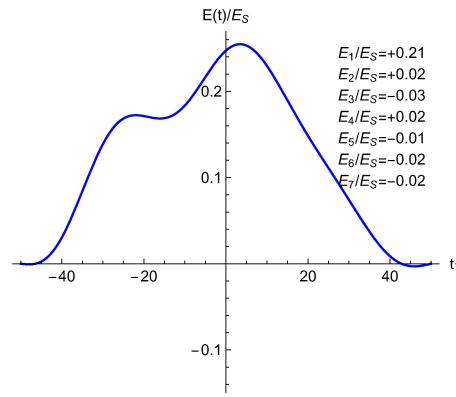
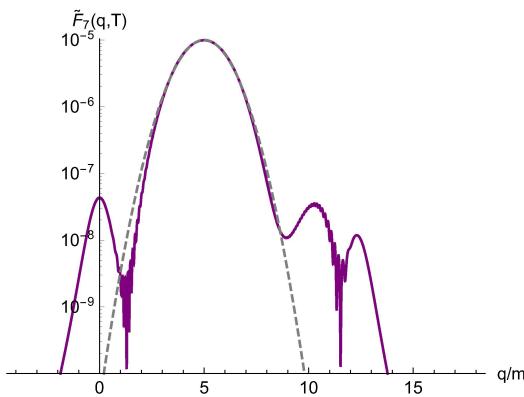
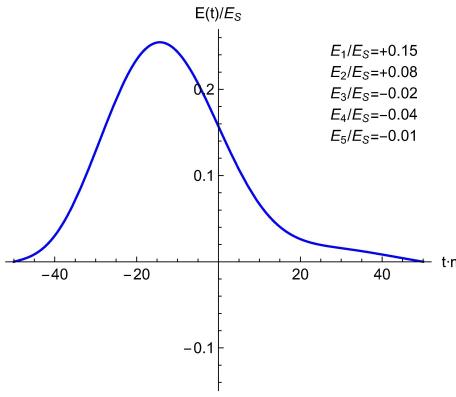
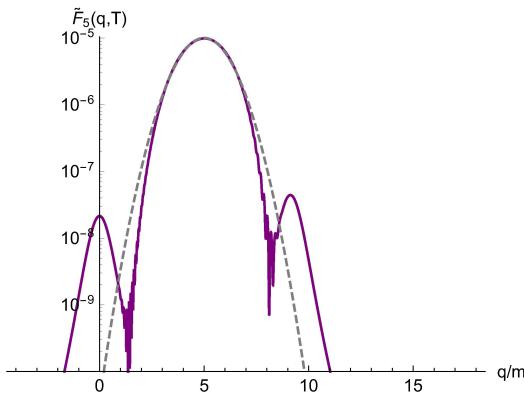


landscape with several
stationary points

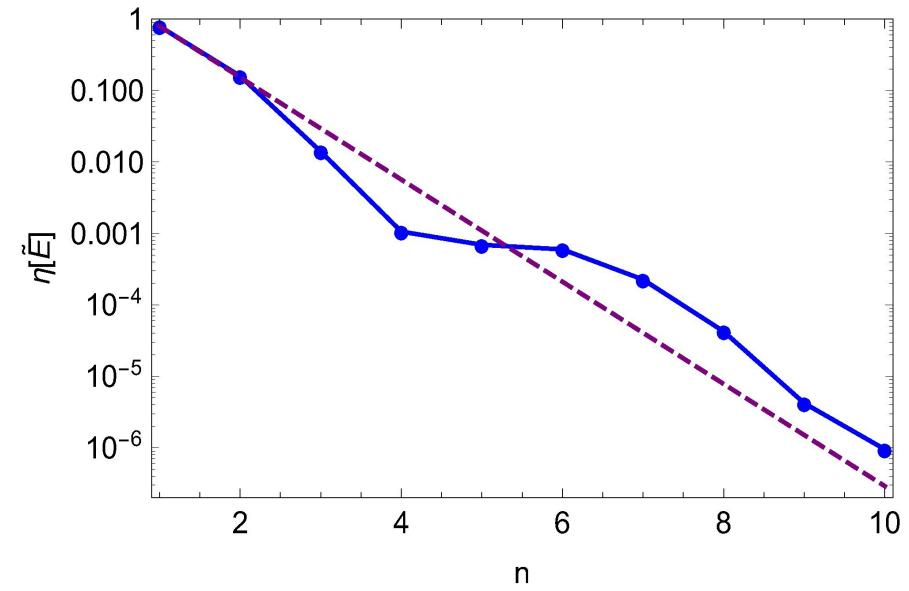
small # of harmonics to
approximate the Gaussian peak



convergence properties



convergence towards
objective distribution



exponential improvement
as function of n

pulse shape optimization for rotating fields

Fillion-Gourdeau, FH, Gagnon, and MacLean, *Pulse shape optimization for Schwinger pair production in rotating fields*, PRD 96 (2017)

pulse shape optimization

maximize the particle number for given fluence (energy density)

- improvements/extensions:
 - field configurations: 2d (rotating) fields [dynamical system: 6 ODE]
 - pulse parametrization: polynomial basis expansion (B-splines)
- parametrization by spectral density $E_k(\omega)$ & phase $\varphi_k(\omega)$ [$k=2,3$]

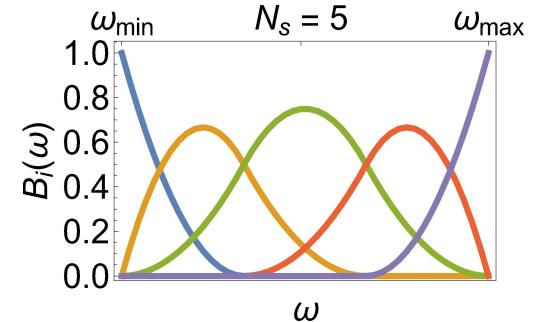
$$E_k(\omega) = \sum_{i=1}^{N_s} a_{k,i}^{(E)} B_i(\omega)$$

(i) compact support

$$\varphi_k(\omega) = \sum_{i=1}^{N_s} a_{k,i}^{(\varphi)} B_i(\omega)$$

(ii) positive definite

(iii) easy to implement



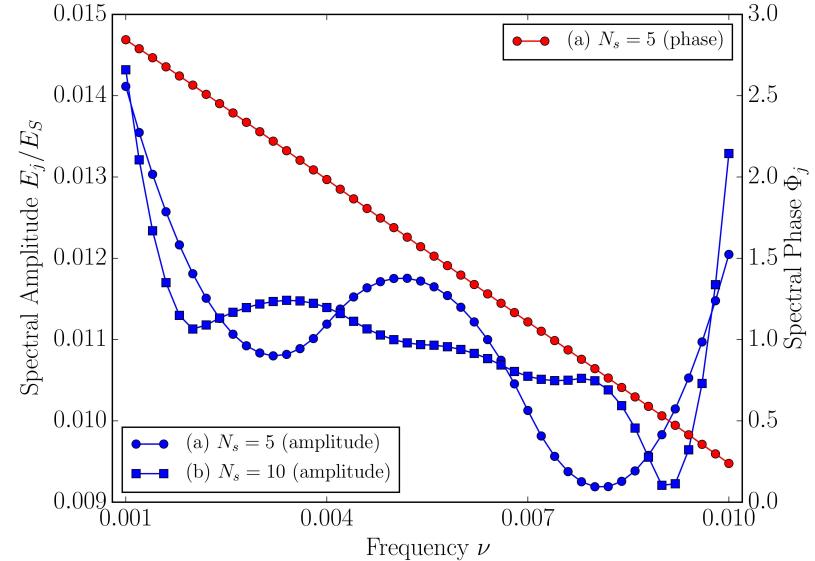
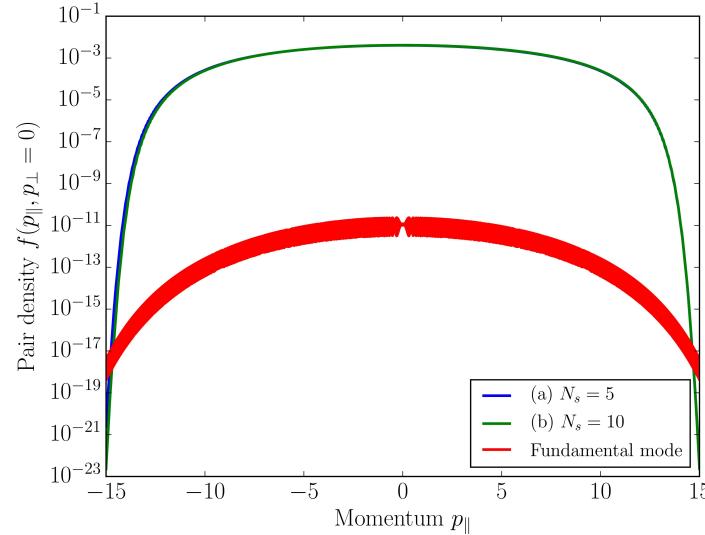
control function: $E_k(t) = f(t) \sum_{j=0}^{n_\omega \sim 50} E_{k,j} \cos(\omega_j t - \varphi_{k,j})$

cost functional: $J = \int_{-T}^T [dq] F(q, T)$

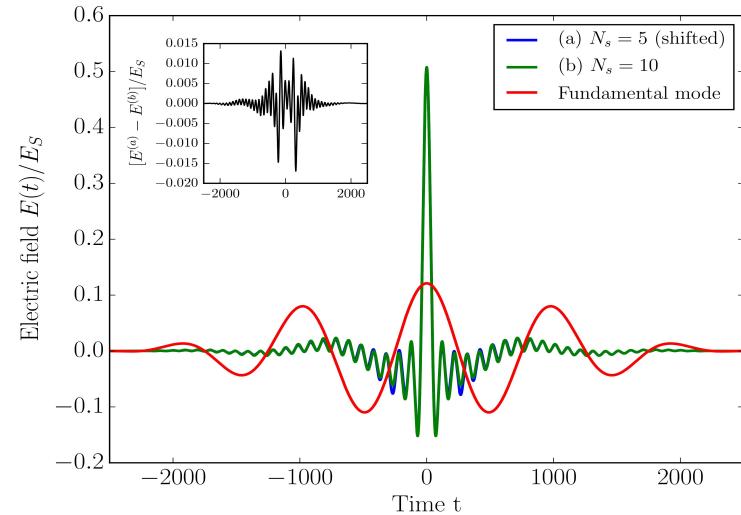
constraint: $\int_{-T}^T dt \vec{E}^2(t) = const$

quality of B-splines ($d=1$)

of components: $n_\omega = 45$
 min. freq.: $\omega_{\min} = 2\pi / 1000$
 max freq.: $\omega_{\max} = 2\pi / 100$



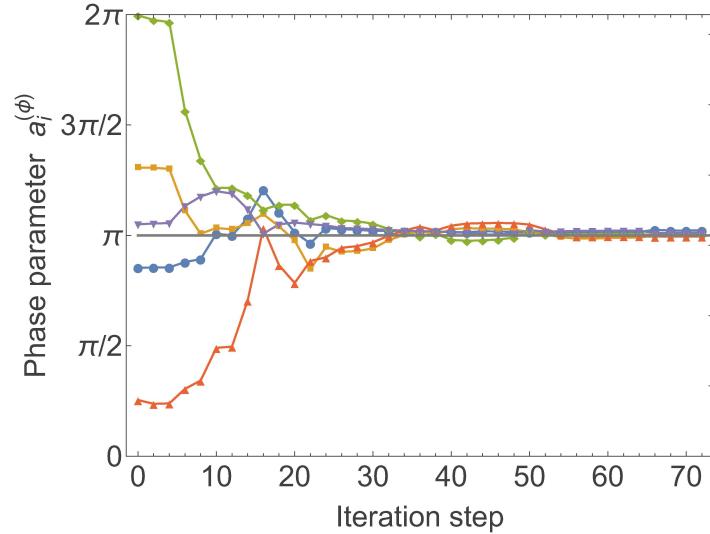
- optimum = reduction of interferences
- $N_s = 5/10$ basically identical
- $\varphi(\omega) \sim \omega$ [irrelevant time shift $\rightarrow 0$]
- $E(\omega)$ unique for fixed N_s
- $N_s = 5/10$ substantial deviations
- optimum = reduction of pulse duration
- $N_s = 5/10$ basically identical [max. 3%]



B-splines: $N_s = 5$ captures physics of $n_\omega = 45$ modes

polarization effect (d=2)

of components: $n_\omega = 50$
 min. freq.: $\omega_{\min} = 4\pi / 100$
 max freq.: $\omega_{\max} = 6\pi / 100$



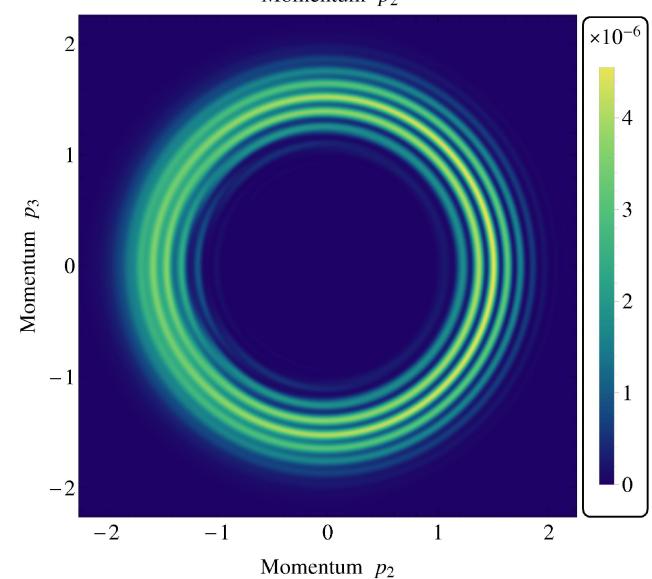
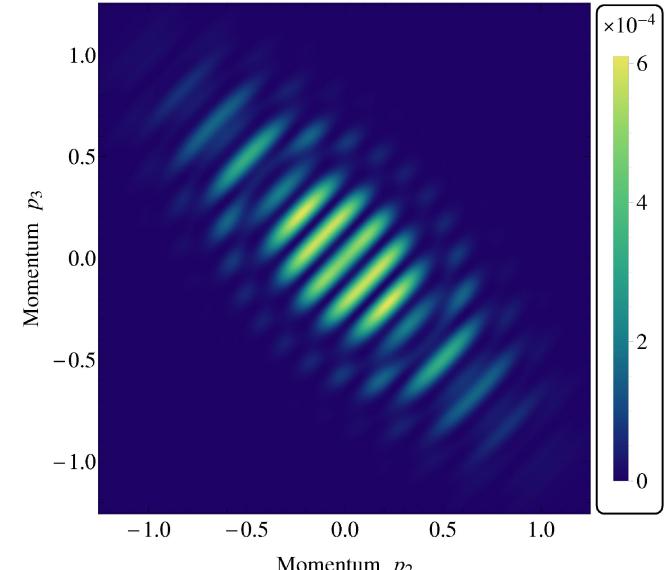
- for fixed $a_{2,i}^{(\varphi)} = 0$, relative phase $a_{3,i}^{(\varphi)} \rightarrow \pi$
- all **ellipticities vanish**
- **optimum = linear polarization**

linear polarization

- orthogonal decay
- peaked at $p = 0$
- max. $\sim 5 \times 10^{-4}$

circular polarization

- ring structure
- peaked at $p/m = 1.5$
- max. $\sim 5 \times 10^{-6}$

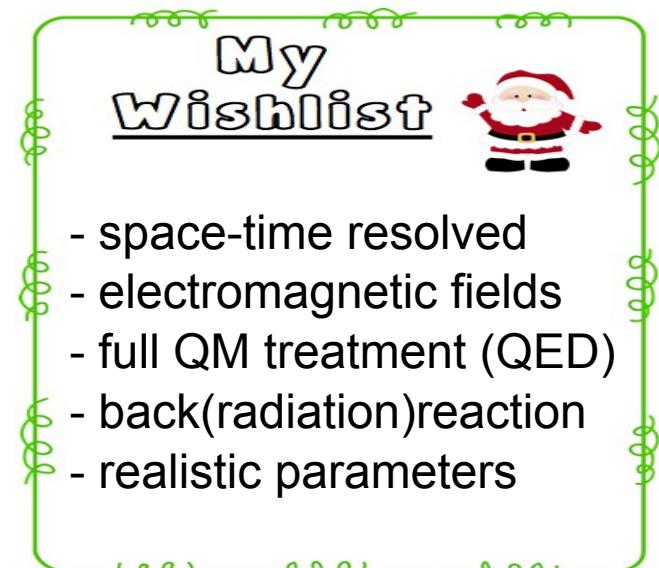
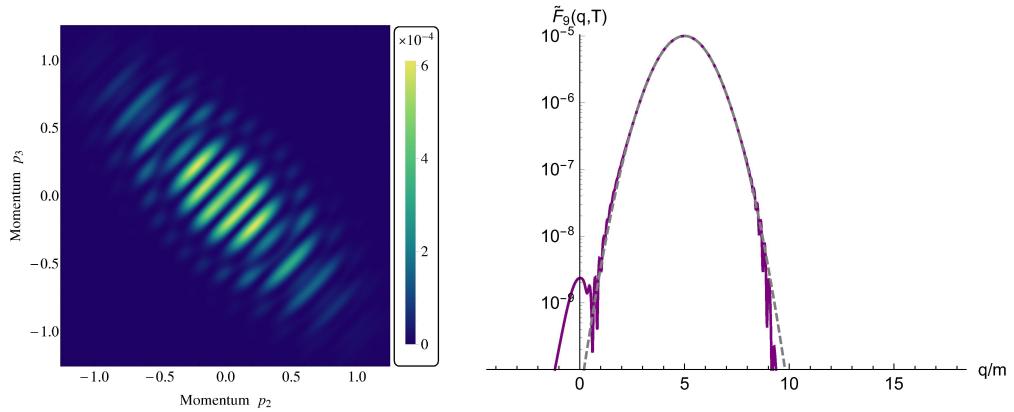


linear polarization is superior for fixed fluence

conclusions & outlook

take-home lessons

- optimization: powerful tool for studying dynamical processes
 - pulse shaping: which field profile maximizes particle production for given energy
 - inverse problem: which field profile leads to a given distribution $F_0(q)$
 - ...
- shortcomings / open problems
 - realistic experimental situation: is the control sufficient to make use of these predictions?
 - more realistic simulations necessary (field parameters & configurations)



Thank you!